Virtual Face Image Generation For Illumination And Pose Insensitive Face Recognition

Wen Gao¹⁴, Shiguang Shan¹, Xiujuan Chai², Xiaowei Fu²
 ¹Institute of Computing Technology, CAS, P.O.Box 2704, Beijing, China, 100080
 ²Department of Computer Science, Harbin Institute of Technology, Harbin, China, 150001

ABSTRACT

Face recognition has attracted much attention in the past decades for its wide potential applications. Much progress has been made in the past few years. However, specialized evaluation of the state-of-the-art of both academie algorithms and commercial systems illustrates that the performance of most current recognition technologies degrades significantly due to the variations of illumination and/or pose. To solve these problems, providing multiple training samples to the recognition system is a rational choice. However, enough samples are not always available for many practical applications. It is an alternative to augment the training set by generating virtual views from one single face image, that is, relighting the given face images or synthesize novel views of the given face. Based on this strategy, this paper presents some attempts by presenting a ratio-image based face relighting method and a face re-rotating approached based on linear shape prediction and image warp. To evaluate the effect of the additional virtual face images, primary experiments are conducted using our face specific subspace method as face recognition approach, which shows impressive improvement compared with standard benchmark face recognition methods.

1. INTRODUCTION

Face recognition has attracted much attention in the past decades for its wide potential applications in commerce and law enforcement, such as mug-shot database matching, identity authentication, access control, information security, and surveillance. Much progress has been made in the past few years [1,2].

Since the 1996s, appearance based methods have been dominant researches, from which two FRT categories were derived: bottein appearance feature based and analysic local feature based. Popular methods belonging to the former paradigm include Eigenface(3). Flisherface(4). Local Feature Analysis (LFA/J) and Elastic Bunch Graph Maching (EBOM)(6) are typical instances of the latter category. In recent years, Eigenface, Fisherface, EBGMel (ASSM/AAM)(7, 22), subspace discrimination analysis(BS) and SVM(III) based approaches have attraction. FERET evaluation has provided extensive comparisons of these algorithms [9].

However, face recognition remains a difficult, unsolved problem in general. The performance of almost all current face recognition systems, both best academic systems and most successful commercial systems, is heavily subject to the variations in the imaging conditions. It has been discovered by the FERET and FRVT test that pose and illumination variations are among the several bottlenecks for a practical face recognition system [9]. By far, no revolutionary practical solutions are available for these problems. However, some solutions to pose and illumination problems do have emerged including invariant feature based methods [16], 3D linear illumination subspace [4], linear object class [11], illumination and pose manifold [12], Symmetric Shape-From-Shading [8], photometric alignment [13], Quotient Image [14], illumination cones [15], Lambertian Reflectance and Linear Subspace [17], Eigen light-fields [18] and parametric linear subspace [19].

Generally, we may categorize approaches used to cope with variation in appearance into three kinds: invariant features, canonical forms, and variation modeling [20]. The first approach seeks to utilize features that

invariant to the change in the distribution of such representation, considered in preparamet. Examples of such representation, considered in the considered images convolved maps, image intensity derivative transpose convolved with 2D Gabo-considered in such considered in the considered in the considered in the considered in sufficient by itself to overcome image variations because of a change in the direction of himmanistor in Cl. Most recently the Quotient Image [14] is reported to be invariant to illumination and may be used to recognize faces when lighting conditions, changes

The second approach attempts to "normalize" away the variation in appearance, either by image transformations or by synthesizing a new image from the given image in some canonical form. Recognition is then performed using this canonical form. Examples of this approach include [8, 21].

The idea of third approach, variation modeling, is to learn, in some suitable subspace/manifold, the extent of the variation in that space/manifold. Recognition is then conducted by choosing the subspace/manifold closest to the novel image. Currently, this paradigm has been recognized as the dominant one among the three approaches[11, 12, 13, 15, 17, 19, 20].

In this paper, we investigate the possibility to augment the training set for modeling the variations by generating virtual face images when changing lighting conditions or viewpoints. This is especially useful for applications that only limited samples per face are available for training.

The paper is organized as: In section 2 we first described briefly our works on ASM for a ligning face images. Section 3 describes the ratio-image based face relighting approach, followed by virtual view prediction based on shape prediction. Our recognition approach based on Face Specific Subspaces (FSS) is presented in section 5. Experiments are set up in the last section.

2. Our Works On Feature Correspondence

Both our face relighting method and face rotating method need accurate feature correspondence. Therefore, we first describe our works on feature extraction briefly. Refer to [23], [24], [25] respectively for details of our work on face segmentation, eye localization and face shape extraction. Our face detection method, named Face Center-of-Gravity Template, is based on some observations on the configure relationship between major face organs. The eyes are then localized by growing a region window from the approximate center of the detected face and checking its characteristics. After eyes are located, we attempt to combine the ASM's local texture models and AAM's global appearance models for spare facial feature correspondence. To integrate the local profile and global appearance constraints, the subspace reconstruction residual of the global texture is exploited to evaluate the fitting degree of the current model to the novel image. And, similar to the AAMs, global texture is used to predict and tune the model parameters. Some results of our feature extraction method are shown in Fig.1.



Figure 1. Results of our feature correspondence
3. Ratio-Image Based Face Relighting for Modeling
Illumination Variations

In this section, a ratio image based face relighting method is presented. The method is based on the assumptions that any face were a convex surface with a Lambertian function, that is, a face image can be described by the product of the albedo and the cosine angle between a point light source and the surface normal:

$$I(x,y) = \rho(x,y)\vec{n}(x,y) \cdot \vec{s}$$

where $\rho(x,y)$ is the albedo associated with point x,y in the image, $\vec{n}(x,y)$ is the surface normal direction associated

with point x,y in the image, and \overline{s} is the point light source direction and whose magnitude is the light source intensity.

Thus, our problem can be formulated as: Given a face image I_0 under normal light source, \overline{s}_0 , we need to relight the face under other light sources, e.g. \vec{s}_j . To solve this problem, we present a ratio-image based method,

First, we define the ratio-image for the i^{th} face (person) under the k^{th} light source as:

is source as:

$$r_{ik} = I_{ik} / I_{i0}$$

 $= (\rho_i \vec{n}_i \cdot \vec{s}_k) / (\rho_i \vec{n}_i \cdot \vec{s}_0)$
 $= (\vec{n}_i \cdot \vec{s}_k) / (\vec{n}_i \cdot \vec{s}_0)$

where ρ_i is the albedo (surface reflectance) associated with the i^{th} face, \vec{n}_i is the corresponding surface normal directions, and \vec{s}_0 and \vec{s}_i are the standard and target point light source directions respectively. Thus, we have:

$$I_{ik} = \rho_i \vec{n}_i \cdot \vec{s}_k = (\rho_i \vec{n}_i \cdot \vec{s}_0) \otimes r_{ik} = I_{j0} \otimes r_{ik}$$
, where \otimes denotes Cartesian product. This means that, given the ratio-image and the standard that it is means that,

where Θ denotes Cartesian product. This means that, given the ratio-image and the standard face image, we can relight the face to the k^{th} light source.

The ratio-image above defined is almost useless since it is only applicable to the # face. However, notice that all faces have similar 2D and 3D shapes, so ne can try to first warp all faces to the same shape and these tomputs the ratio-image for religiting the standard fleer tomputs the test of the same shape and the standard fleer to the same shape and the standard fleer to the same shape. Currently, we just warp the 2D face image to a predefined mean shape, as defined in ASM. After the warp procedure, all face images are expected to have quite similar 3D shape. Therefore, given a training set, by warp all the face images under different lighting conditions to the same shape, we can define the universal ratio-image for the 6* light source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the mean of all the specific ratio-image of the Asm of the single source as the single source as the single source source as the single source source source as the single source source

$$R_{k} = \frac{1}{N} \sum_{i=1}^{N} \frac{T_{ik}}{T_{i0}} = \frac{1}{N} \sum_{i=1}^{N} R_{ik}$$

where N is the total faces in the training set, T_{ik} is the shape-free texture warped from the t^{ik} face images lighted under the t^{ik} light source, and T_{i0} is its corresponding texture under the standard light source.

By varying the different light source, we can get the ratio-image for each light source and/or combine them to ratio-image for any lighting conditions.

After the ratio-images are computed, any novel face image I_0 with standard lighting conditions can be relit by the following procedure:

- Find the face in the picture and extract its 2D face shape using the method descried in Section 2:
- Warp the face to texture T₀ according to the predefined mean shape;

 Relight the face image under k-th lighting condition according to the k-th ratio-image by:

$$T_k = T_0 \otimes R_k$$
;

 Reverse-warp the texture T_k to its original shape to get the relit image I_k;

Fig. 2 illustrates some relighting effect of our method on the Yale face Database B (The other 9 person's faces are used to compute the 63 ratio-images for 63 light sources).







Olinyui immer (v)Labeled landmarks (e)Masked im

(d) Relit images Figure2. Ratto-image based face relighting

4. Virtual View Generation For Different Poses

Similar to face relighting, the virtual view generation problem is defined as: given a frontal view of an unknown face, generating its view under other poses. Let P_0 denote the frontal pose, P_2 be another pose (e.g. right rotating 30° out of the image plane), and I_0 be the image under pose P_0 . Our goal is generating its view I_0 under pose P_0 .

A linear engression method is exploited to solve this problem: a learning set containing pairs of the shapes of the two views under P_0 and P_1 is collected, a linear mapping between them are learned and applied to any given novel frontal image to preclice its shape under pose P_1 . Let $\mathbb{X} = \{(I_1^0, I_1^1), (I_2^0, I_1^1), \cdots, (I_p^0, I_p^1)\}\}$ be a minage set containing pairs of the two views under P_0 and P_1 , and $\mathbb{X} = \{(S_1^0, S_1^0), (S_2^0, S_2^1), \cdots, (S_n^0, S_n^0)\}\}$ be the corresponding shape set containing pairs of the shapes for the two views in the learning set \mathbb{X}^1 . A linear mapping P can be learnt easily from \mathbb{X}^1 . So, for a given novel image \mathbb{X}^1 under pose, P_0 , its shape vector \mathbb{X}^1 is first extracted using method in Section 2. Then, its face shape \mathbb{X}^1 viewed under pose P_1 is predicted by:

 $S^1 = PS^0$

Then we can generate the virtual view by an image warping procedure based on S" and S'. Fig.3 shows two examples of the generation results, in which the first row

are the original frontal views with landmarks overlapped; the second row is the generation results.



Figure 3. Virtual view generation

5. FSS-based Face Recognition

In our previous work, we have proposed a Face-Specific Subapace (FSS) based face recognition method [26]. This method is motivated, but essentially different from the traditional Eigenface. In Eigenface, each face image is represented as a point in a low dimensional face subspace thaterd by all faces; however, we experimentally show that one of the dements of such as tataety is that the most discriminant features of a specific face are not accurately represented. Therefore, we propose to model each face by one individual face subspace, named Face-Specific outpace, that is, the reconstruction error, is then exploited as the similarity measurement for identification.

Each FSS is learnt from the training images of the specific face and represented as a 4-tuple by:

$$\mathfrak{R}_k = (U_k, \Psi_k, \Lambda_k, d_k),$$

where U_i is the eigenvector matrix. Λ_k is the eigenvalues, Ψ_i is the mean of the k^{th} face, and d_k is the dimension of the FSS.

Similar to DFFS in Eigenface method, the similarity of any times to a face can be measured by using the Distance from FSS (DFFSS) less DFFSS means more probability that the image belongs to the consequence of the constant of the projected to the k^{Λ} FSS by, $H^{\Lambda(1)} = U_1 / \Phi^{\Lambda(1)}$, where $\Phi^{(1)} = \Gamma_1 - \Psi_1$. Then $\Phi^{(1)} = 0$, $\Gamma_2 - \Phi^{(1)}$ is constructed by, $\Phi^{(1)} = U_1 H^{\Lambda(1)}$. So, Γ 's distance from k^{Λ} FSS (DFFSS) is computed as the following reconstruction error:

The DFFSS can be regarded as the similarity of the input pattern Γ to the face corresponding to the k^{th} FSS. Therefore, the following minimal distance classifier can be naturally formulated:

$\Gamma \in \Omega_m$ if $\varepsilon^{(n)} = \min{\{\varepsilon^{(k)}\}}$

6. Experiments on Yale Face Database B

To evaluate the effect of augmenting training set for face recognition, we conduct experiments on the Yale Face Database B (Refer [15] for detailed information on this face database). We choose just the frontal set in this DB, containing 640 images from 10 persons, each person has 64 frontal images under 64 different lighting conditions. To test different face recognition methods, we choose the frontal face image under the standard lighting of each person as training images, other 63 images lighted under different for testing.

Leave-one-out strategy is exploited to generate the ratio-image for each lighting configure. Then, 63 additional face images from each standard lighting face images are generated to augment the training set for the FSS method. The testing results on the 5 subsets are shown in Fig. 4.(Note: other methods tested are correlation. PCA and Facelt3.0 system. They do not using the additional virtual images for train).

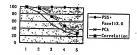


Figure 4. Performance comparison on the 5 subsets i the Yale Face Database B

From Fig.4, a significant performance improved can be observed, which obviously profits from the augment of the training set.

Acknowledgements

This research is sponsored partly by NSF of China (No.69789301), National Hi-Tech Program of China (No.2001AA114190), and YinChen Net. Co.

REFERENCES

- [1] R. Brunelli and T. Poggio, "Face Recognition: Features versus Template", TPAMI, 15(10), pp1042-1052, 1993 [2] R.Chellappa, C.L.Wilson ect. "Human and Machine
- Recognition of faces: A survey", Proc. of the IEEE, 83(5), pp705-740, 1995,5 [3] M.Turk and A.Pentland. "Eigenfaces for Recognition"
- Journal of cognitive neuroscience, 3(1), pp71-86, 1991.1 [4] P.N.Belhumeur, J.P.Hespanha and D.J.Kriegma
- "Eigenfaces vs Fisherfaces: recognition using class specific linear projection". TPAMI, vol.20, No.7, 1997.7
- [5] P.Penev and J.Atick, "Local Feature Analysis: A General Statistical Theory for Object Representation," Network:

- Computation in Neural Systems, vol.7, pp.477-500, 1996
- [6] L. Wiskon, J.M.Fellous, N.Kruger and C.V.D.Malsbur, "Face Recogniton by Elastic Bunch Graph Matching", IEEE Trans. On PAMI, 19(7), pp775-779, 1997.7
- [7] T.F.Cootes, G.J.Edwards, C.J.Taylor, "Active Appearance Models", ECCV, vol.2, pp484-498, 1998.
- [8] W.Zhao and R.Chellappa, "Robust Image-Based 3D Face Recognition", CAR-TR-932, N00014-95-1-0521, CS-TR-4091, Center for Auto Research, UMD, 2000.1
- [9] P.J.Phillips, H.Moon, etc. "The FERET Evaluation Methodology for Face-Recognition Algorithms", IEEE TPAMI, Vol.22, No.10, pp1090-1104, 2000
- [10]G.Guo, S.Z.Li and K.Chan, "Face Recognition by Support Vector Machines", FG'02, pp196-201, Grenoble, 2000.3
- [11]T.Vetter and T.Poggio, "Linear Object Classes And Image Synthesis From A Single Example Image", IEEE Trans. On PAMI, Vol.19, pp733-742, 1997
- [12]H.Murase, S.Nayar, Visual Learning and recognition of 3D object from appearance, IJCV, 14:5-24, 1995
- [13]A.Shashua, On Photometric Issues in 3D visual recognition from a single 2D Image, International Journal of Computer Vision, 21(1/2), 99-122, 1997
- [14] A.Shashua and T.Riklin-Raviv, "The Quotient Image: Class-Based Re-Rendering And Recognition With Varying Illuminations", IEEE Trans. on PAMI, pp.129-139, 2001.2
- [15]A.S.Georghiades, P.N.Belhumeur and D.J.Kriegman, From Few to Many: Illumination Cone Models for Face Recognition under Differing Pose And Lighting", IEEE TPAMI, Vol.23, No.6, pp643-660, June 2001
- [16]Y.Adini, Y. Moses, S.Ullman, Face Recognition: The Problem of Compensting for changes in illumination Direction, IEEE TPAMI. Vol.19, No.7, pp721-732, 1997
- [17] R.Basri, D. Jacobs, Lambertian Reflectance and Linear Subspaces, ICCV2001, Beckman Institute, Vol.2, p383-390. 18]R.Gross, I.Matthews, S.Baker, Eigen Light-Fields and Face Recognition Across Pose, Proc. of FG02
- [19]K.Okada, C.Malsburg, Pose-Invariant Face Recognition with Parametric Linear Subspaces, Proc. of FG02
- [20]T.Sim, T.Kanade, Combining Models and Exemplars for Face Recognition: An Illuminating Example, in Proceedings of Workshop on Models versus Exemplars in Computer Vision, CVPR 2001.
- [21]P.J.Phillips, Y.Vardi, Efficient Illumination Normalization of Facial Images", PRL, 17(1996), 921-927
- [22]T.F.Cootes, C.J.Taylor, D.Cooper, and J. Graham. Active shape models-their training and application. Computer vision and image understanding, 61(1): pp38-59, 1995.
- [23]J.Miao, H.Zhang, W.Gao, et al., FaceTracker: A Human Face Tracking and Facial Organ Localizing System, the Proc. of the 8th ICCV, Cananda July.2001 pp.743-743,
- [24]B.Cao, S.Shan, W.Gao, D.Zhao. Localizing the ins center by region growing search. Proc. of the IEEE ICME 2002.
- [25] W. Wang, S.Shan, W.Gao, B.Yin, Combining Active Shape Models and Active Appearance Models For Accurate Image Interpretation, Submit to ICASSP 2003.
- [26]S.Shan, W.Gao, D.Zhao, Face Identification From A Single Example Image Based On Face-Specific Subspace (FSS), Proceedings of the IEEE ICASSP2002

Short Papers

Online Fingerprint Template Improvement

Xudong Jiang and Wee Ser, Senior Member, IEEE

Abstact—This work proposes a technique that improves lingorprint templates by manying and among print time of multiple fingespinishs. The weighted eveninging scheme resultest the region with time of print and time of the abjorition greatly extended to the abjorition greatly reduces the set with chargest produces the storage and computation required many for abjorition greatly reduces the storage and computation required more than the proposed appoints improvement produced many for a fingerprint verification process. Extensive experimental studies demonstrate the testability of the proposed appoints.

Index Terms—Fingerprint verification, minute set, template improvement, multiple (ingerprints,

1 INTRODUCTION

An automatic fingerprint verification system matches fingerprint inputs with prestored fingerprint templates, each of which consists of a set of features extracted from a fingerprint image. Since the most reliable feature for fingerprint matching is the minutia, most current automatic fingerprint verification systems are based on minutia matching. A fingerprint template of such systems is thus a minutia set. The two most prominent kinds of minutiae are ridge ending and ridge bifurcation, which can be extracted using techniques such as those proposed in [1], [2], [3], [11]. Unfortunately, noise, inadequate contrast, and other image acquisition artifacts often make reliable minutia extraction very difficult. The resulting undesirable results include spurious minutiae being produced, valid minutiae being lost, and the minutia type (ending or bifurcation) being wrongly labeled. The employment of various image enhancement techniques [4], [5] merely alleviate these problems to a limited extent since they operate only on a single fingerprint image. Maio and Maltoni [6] implemented five different minutia extraction techniques [7], [8], [9], [10], and compared their performances. The best technique in their experiment produced 8.52 percent spurious minutize, lost 4.51 percent genuine minutiae, and caused the type labeling error for 13.03 percent minutiae, resulting in a total error of 26.07 percent. For the other approaches, the total errors were 33.83 percent, 119.80 perceni, 207.52 percent, and 216.79 percent, respectively. From this experiment, we can see that perfect minutia extraction from a single fingerprint image is a very difficult task.

Whereas the improvement of minutia extraction from a single fingerprint image is thirtide, multiple fingerprint images carptured at different times can be used to achieve more significant improvements since the imaging conditions that cause the minutia extraction error change with time due to the changes in skin condition, climate, and on-site environment. However, improving the image quality based on multiple fingerprints is unfeasible due to the high memory and computation, consumption required by processing multiple images that are not rotation and translation invariant. Instead, it is more feasible to improve the tamplate minutia set by using multiple minutia sets of fingerprints captured at different times. If this template improving process requires only a small memory spaceand short computation time, it can be performed online in a fingerprint verification system, which receives fingerprint inputs of uses:

 The authors are with the Centre for Signal Processing, Nanyang Technological University, 50 Nanyang Avenue, Singapore 639798.
 E-mail: lexdjiang, esser@ntu.edu.eg.

Manuscript received 7 Mar. 2001; revised 11 July 2001; accepted 17 Oct. 2001. Recommended for acceptance by M. Pietlkninen. For information on obtaining reprints of this article, please send e-mail to: spani@computer.org, and reference (EEEE Stop Number 113757.

0162-6828/02/\$17.00 # 2002 IEEE

during the day-to-day normal operation. Such online template improving functions work by merging the input data into the template database during the actual application of the fingerprint verification system.

This paper proposes an online fingerprint template improvement algorithm with which spurious minutiae can be removed, dropped minutiabe be recovered, and wrongly labeled minutia type be corrected. The proposed algorithm works online during the daylve-day operation of the fingerprint verification system. As a result, users will find the system more and more reliable.

2 MINUTIA SET ESTIMATION FROM MULTIPLE MINUTIA SETS

To extract the minutise, the image outputted from a fingerprint ensemble as essentials to be segmented into the background (invalid fingerprint region) and the valid fingerprint region) and the valid fingerprint region and the part of a finger. Thus, different fingerprint image explained from the same finger usually have different (valid) fingerprint region on the represented by a point set, which contains x- and y-coordinates of all pixels within this region. Suppose that we have M fingerprint images captured from the same finger and obtained M minutis sets $\mathbb{P}^m = \{F_p^m\}$ and fingerprint regions \mathbb{S}^m by applying an minutia extraction algorithm [11], where

$$F_k^m = (x_k^m, y_k^m, \varphi_k^m, t_k^m)$$
 (1)

is a parameter vector describing the location [x**, y**, b), the direction y** and the type (\$\frac{0}\) minutes he in fingerprint: \(m\). Although the position and direction of a finger on the sensor is usually related to the various acquisitions, pose transformation on his perification of the transformation on his perification of the properties of t

For a particular physical minuta, we obtain M sample measurements of the parameter vector from M different fingermins ($M \le M$). Our task is to estimate an optimal parameter vector based on these M measurements, i.e., learning from samples of experimental data. This problem could be approached in the context of minimizing a suitable cost function. If the cost function is those to be the negative logarithm of the likelihood function derived from the sample data, this becomes equivalent to maximum likelihood (M), learning, by considering a generalization of the Gaussian distribution of the data with a constant variance, the M Lapproach leads to a cost function of the form

$$E = \sum |F_k^m - F_k^p|^R,$$

known as the Minkowski-R error [13], where F_k^T is the optimal representative minuta parameter vector to be estimated. When the distribution of the data is assumed to be standard Gaussian, i.e. R = 2, the cost function reduces to the sum-of-squares error. If a Laplacian distribution is assumed, i.e., R = 1, the cost function of the cost function is a surface, i.e., R = 1, the cost function is the cost of the cost o

since minutiae with large measurement errors cannot be matched with other corresponding minutiae with small measurement errors. This provides the notivation in using the sum-of-squares error as the cost function.

Although the biological characteristics of fingerprints ensure minutia features to be permanent and unchanging for a given finger [1], acquisition of minutiae information is affected by the skin and imaging conditions at the time of measurement and the exact manner the finger was making contact with the sensor. As a result, the measured minutia parameter inevitably changes with time and the measurements F_k^m can thus be seen as a temporal sequence of data. As such, the machine-learning task could be viewed as a problem of regression estimation, i.e., function or model learning. There are a number of well-developed approaches in the literature for these problems, for example, LPC [15], Kalman filtering [16], Hidden Markov model [17], MCMC methods [18] and EM-C algorithm [19]. However, changes to minutia parameters may occur abruptly with these changes being maintained for quite a long time due to the skin nature and human's habits. F_{k}^{vo} is thus typically an abrupt rather than a smooth function of m, which makes it difficult to apply the abovementioned function learning approaches. Furthermore, fingerprint samples for a particular user are not collected in even time intervals; duration between two subsequent presentations of a finger to the system may vary between several minutes to several months. This again makes the above-mentioned approaches unsuitable

Having considered the above factors and the computational efficiency required for an online application, we employ the weighted least-squares with predetermined weights as the learning rule. The weights are chosen based on the nature of minutia set series, the objective of the integration of the multiple minutia sets, and the computation efficiency. For instance, a higher weight should be assigned to the registered template than the query fingerprint received in the verification process since the original template obtained during the registration phase is generally more reliable than the input minutia sets obtained during the day-to-day verification process. More recent fingerprint inputs should also be assigned with higher weights than earlier ones since the integration of the multiple minutia sets is aimed at increasing the reliability of future matching process. The weights will be chosen in the next section based on these desired factors and the computational resources required.

The estimation errors for all minutiae k of all minutia sets m are expressed as

$$e_k^m = F_k^m - F_k^p$$
, for $\forall (k, m)F_k^m \in \mathbb{F}^m$.

The estimated minutia F_k^{ℓ} is obtained by minimizing the weighted sum of the squared errors

$$\sum_{m,F_k^m \in \mathbb{F}^n} w_k^m (\varepsilon_k^m)^2 = \sum_{m,F_k^m \in \mathbb{F}^n} w_k^m (F_k^m - F_k^p)^2$$

$$\Rightarrow \text{Minimum, for } \forall k, F_k^m \in \mathbb{F}^m.$$
(3)

where w_i^m are predetermined weights. Based on this criterion, it is straightforward to obtain $E_i^T = \frac{1}{1 + \frac{1}{2}} \sum_{i} w_i^m E_i^m - \frac{1}{2} \exp(i \sum_{i} x_i \nabla_i x_i^m) = \frac{1}{2} \exp(i \sum_{i} x_i \nabla_i x_i^m)$

$$F_k^P = \frac{1}{\sum_{m,F_k^m \in \mathbf{F}^m} w_k^m} \cdot \sum_{m,F_k^m \in \mathbf{F}^m} w_k^m F_k^m, \quad \text{for } \forall k, F_k^m \in \mathbf{F}^m. \tag{4}$$

The above estimated minutia parameter F_k^p generally has better accuracy than F_k^p since it is a weighted arithmetic average over all matched minutiac. As a result, wrongly labeled minutiae type can be statistically corrected during the averaging process.

If all estimated minutiae by (4) are collected in the estimated tempolae, a tempolae synthesis will be performed. If we match an input fingerprint with this template, we will fine the problem of matching a partial input fingerprint with a much larger full fingerprint. Paths on command the may decrease but false match rate may increase simultaneously, or some matching criteria have to be changed by compromise. Further, template synthesis can be simply to the property of the

offline performed by enrolling several fingarprints for each finger and there is no point in online synthesizing the templates. The problem of the template synthesis was addressed in [20]. This works not atimed at solving the problem that the template represents only a partial fingarprint, but aimed at improving the quality of the template conline, i.e., reducing the minutia extraction error. Thus, our estimated template is restricted to an estimated ingerprint region S', which can be chosen to be one of the M original fingarprint regions S' or be determinedly the synthesized fingarprint region in case the template synthesis is performed beforehand in the registration obtains.

Our estimated minutia set $F' = \{P_i''(x_k'', y_k'') \in S''\}$ contains all mutuals in the region S'' extracted from the M fingerprints. As a result, genuine minutals that are not extracted from some fingerprints can be recovered in the estimated minutia set F' if they are successfully extracted from some other fingerprints. However, any spurious minutia extracted from any fingerprint is also transferred in the estimated minutia set if it is located within S''. Therefore, a technique has to be developed to identify the spurious minutia extracted from the estimated minutia set if it is located within S''. Therefore, a technique has to be developed to identify the spurious minutiae of the estimated menglace F''.

If an estimated minutia k is successfully extracted from fingerprint m, a certainty level $e_n^n = 1$ is defined. If this minutia fails to be extracted from fingerprint m but its location is within this fingerprint region, a certainty level $e_n^n = 0$ is defined. However, if the region of fingerprint m does not cover this minutia, no information about the reliability of minutia k is provided by fingerprint m. Thus, the reliability of each estimated minutia is described by M certainty levels defined by

$$c_k^{m} =$$

$$\begin{cases}
1, & \text{if } F_k^m \in \mathbb{F}^m \\
0, & \text{if } F_k^m \notin \mathbb{F}^m \land (x_k^p, y_k^p) \in \mathbb{S}^m, \\
\text{unknown, } & \text{if } (x_k^p, y_k^p) \notin \mathbb{S}^m, \\
\text{for } \forall k, F_k^p \in \mathbb{F}^p, m = 1, 2, ..., M.
\end{cases}$$
(5)

Similar to the calculation of the estimated minutia parameter in (4), a certainty level c_k^p of the estimated minutia k can be estimated by the weighted average of c_k^m over all fingerprints whose regions cover the minutia k

$$c_k^{\nu} = \frac{1}{\sum_{m,k_k^{\nu},k_k^{\nu} \in \mathbb{S}^m} w_k^n} \cdot \sum_{m,k_k^{\nu},k_k^{\nu} \in \mathbb{S}^m} w_k^m c_k^m, \text{ for } \forall k, F_k^{\nu} \in \mathbb{F}^{\nu}.$$
 (6)

For authenticating a future input fingerprint, only the minutiae whose certainly levels are equal to or higher than a threshold CN of CN of N in the same than include the contraction of N in the same than include with certainly levels lower than in the template finger of the further template improvement in the final in the template for the further template improvement in the first three template improvement in the first three templates improvement in the same of the further template improvement in the first further template improvement in the further template in the further template improvement in the further template in the furthe

If we choose equal weights, the estimation of a minutia based on (4) and (6) is simplified to

$$F_k^{\mathcal{P}} = \frac{1}{M_b} \cdot \sum_{m, F_k^{\mathcal{M}} \in \mathbf{F}^m} F_k^m, \text{ for } \forall k, F_k^m \in \mathbf{F}^m,$$
 (7)

$$c_k^P = \frac{1}{N_k} \cdot \sum_{m,l,k',k''k'',\mathbf{F}^{n}} c_k^{nl}, \text{ for } \forall k, F_k^P \in \mathbf{F}^{P}.$$
 (8)

where M_s is the number of fingerprints from which minutia k is extracted and N_s is the number of fingerprints that cover the position of minutia k. In this case, we see that it is the minutia occurrence frequency that is used to recover dropped minutiae and remove spurious minutiae.

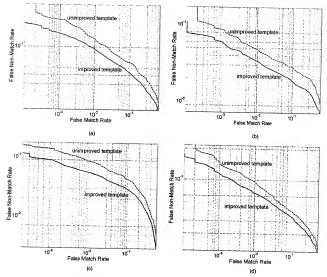


Fig. 1. ROC curves on (a) DB1 a, (b) DB2 a, (c) DB3 a, and (d) DB4 a.

3 ONLINE FINGERPRINT TEMPLATE IMPROVEMENT

It is not user-friendly to capture a number of fingerprints of the same finger at long intervals in the registration phase. However, during the verification operation of a fingerprint verification system, input fingerprints are successively received and compared with the templates. If an input fingerprint is successfully matched with a template, these two fingerprints are verified to have originated from the same finger. Therefore, input fingerprints can be used to improve the matched template online during the day-to-day operation of the fingerprint verification system. However, to use (4) and (6) to improve a template, all matched input minutia sets and fingerprint regions need to be stored and an arithmetic average over all matched minutia sets need to be calculated for every template update. This requires a large storage space and significant computation time. However, storage space and verification time are often serious constraints, especially in stand-alone application. To reduce the storagespace and processing time requirements, we need a simplified fingerprint region representation and a recursive algorithm.

It is not difficult to simplify the fingerprint region representation. A polygon represented by a few points can be used to approximate a fingerprint region [21] and to determine whether a minutia point of another fingerprint is located within this region. It is easy to prove that a point with location (x, y) is within a polygon represented by L points (x_j, y_j) , $j = 1, 2, \dots L$, if and only if:

$$A_jx + B_jy + C_j < 0$$
, for all $j, j = 1, 2, ..., L$, (9)

where
$$A_j = y_j - y_{j-1}$$
, $B_j = x_{j+1} - x_j$, and $C_j = -A_j x_j - B_j y_j$ with $(x_{l+1}, y_{l+1}) = (x_1, y_l)$.

A recursive algorithm that implements the weighted averaging in (4) and (6) can be derived by choosing the weights properly. As mentioned earlier, the finger skin and imaging condition changes with time and the template improvement is aimed at increasing the reliability of future matching processes. Thus, the more recent fingerprint inputs should be assigned higher weights than earlier ones. In addition, a fingerprint image is usually equitured with much cost. In addition, a fingerprint image is usually explured with those acquired during the registration process compared with those acquired during the day-to-day verification. Therefore, a higher weight should be assigned to the original registract template. We thus choose a power series are in weight the fingerprint sequence and another constant \(\lambda\) to distinguish the weights of input fingerprints from that of the original template fingerprint.

Let $F_k^{\mu}(N)$ denote the improved template minutia by using an original template minutia $F_k^{\mu}(0)$ and N input minutiac $F_k^{\mu}(n)$ of N input fingerprints, $n = 1, 2 \dots N$, where fingerprint n is received

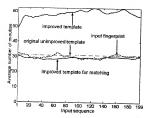


Fig. 2. Average numbers of minutias.

earlier than fingerprint n+1. Without losing generality, (4) can be rewritten as

$$F_k^P(N) = \alpha^N F_k^P(0) + \lambda \sum_{n=0}^{N-1} \alpha^n F_k^I(N-n),$$
 (10)

with the condition of

$$\alpha^{N} + \lambda \sum_{i=1}^{N-1} a^{n} = 1.$$
 (11)

The power series coefficients $\alpha^*(\alpha < 1)$ weight the more recent fingerprint entries more heavily than earlier ones, while the constant $\lambda(\lambda < 1)$ scales the weights of input fingerprints with respect to the original template. By choosing $\lambda = 1 - \alpha$, it is not difficult to prove that condition (11) holds independent of the values of α and λ . Thus, we can use the same value of α in (10) for different number of entries N, i.e., we can have

$$F_k^P(N+1) = \alpha^{N-1}F_k^P(0) + \lambda \sum_{n=0}^N \alpha^n F_k^I(N+1-n).$$
 (12)

From (10) and (12) with $\lambda = 1 - \alpha$, it is straightforward to obtain

$$F_k^P(N+1) = \alpha F_k^P(N) + (1-\alpha)F_k^I(N+1).$$
 (13)

Equation (13) is the recursive template minutis parameter update formula where $P_i^{(\ell)}(N)$ is the old template minutis parameter and $F_i^{(\ell)}(N+1)$ the new template minutis after the fingerprint verification system receives a new reference of the template financiary of the strength of the property of the strength of the streng

In a similar way, a recursive certainty level update formula can be easily derived from (6) as

$$c_k^P(N+1) = \alpha c_k^P(N) + (1-\alpha)c_k^I(N+1),$$
 (14)

where $c_k^P(N)$ is the old certainty level of template minutia k and $c_k^P(N+1)$ the new certainty level of template minutia k after the system receives a new entry with certainty leve $c_k'(N+1)$.

It is worth noting that falsely matched input fingerprints will have an adverse effect on the template improvement process. To reduce the probability of this happening, an input fingerprint is used to update the matched template only if their matching score ms is higher than a threshold Mt that is set to be larger than the verification threshold Mu of a fingerprint verification system. Furthermore, we could limit the shortest this interval TV between

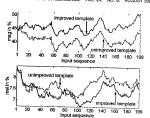


Fig. 3. Average matching scores

two successive updates of a template to prevent any intentional repeated abuse of the template update process. This way, we can diminish the negative effects of the online fingerprint template improvement procedure.

The proposed online fingerprint template improvement algorithm is summarized as follows:

- Users enroll for the fingerprint verification system. For each enrolled fingerprint, a fingerprint region S^p is segmented out and represented by L points and a minutal set {P_i^p} is extracted. A certainty level c^p_i = 1 is initialized for each extracted minutia. Template update time tu is initialized to be the current time tr.
- The fingerprint verification system waits until an input fingerprint is received.
- 3. Segment out the fingerprint region and represent it with L points. Extract input minuths set (F_s^p). Match it with each template (F_s^p(F_s^p) ∈ D_s). If the maximal matching score ms ≤ Mu, reject this input and go to Step 2, otherwise output the corresponding finger ID.
- Read the current time tc. If ms ≤ Mu (Mu > Mv) or tt = tv) ≤ Ti go to Shee 2. If ms ≤ Mu (Mu > Mv) or
- (tc-tu) < Ti, go to Step 2, otherwise tu=tc. 5. The matched template $\{F_k^P\}$ is updated as follows:
 - For all matched template minutiae, F_k^P and c_k^P are updated by

$$\alpha F_k^{\mu} + (1 - \alpha)F_k^I \Rightarrow F_k^{\mu}$$

and $\alpha c_k^p + 1 - \alpha \Rightarrow c_k^p$. b. Find all unmatched template minutiae located within the input fingerprint region by using (9). The certainty levels of these minutiae are updated by $\alpha c_k^p \Rightarrow c_k^p$.

c. The certainty levels of other template minutiae (i.e., those located outside the input fingerprint region) are unchanged, i.e., c_k^p ⇒ c_k^p.

d. Find all unmatched input minutiae located within the template fingerprint region by using (9). Merge these minutiae into the template, i.e., F¹_k ⇒ F¹_k with c¹_k = 1 − α.

e. Remove all template minutiae whose certainty levels are lower than a threshold Cu(0 < Cu < 1 − α < Cv < 1) to limit the enlargement of the template size. Store the updated template and go to Step 2.

The above proposed online fingerprint template improvement algorithm updates a fingerprint template using a recursive algorithm that implements a weighted averaging over all matched fingerprints. It increases the precision of minutia parameter, corrects

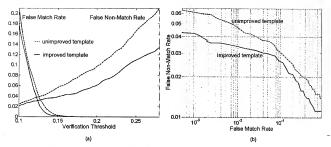


Fig. 4. (a) Paise match rate and false nonmatch rate versus threshold and (b) ROC curves on DB T.

wrongly labeled minute type, recovers dropped minutae (from $e_i^* \subset V$ to $e_i^* \in \mathcal{O}$ b) and removes spurious minuthe (from $e_i^* \subset V$ to $e_i^* \in \mathcal{O}$ b). Buthermore, the algorithm accords greater importance to more recently acquired fingerprins so that it weakens the effect of older skin and imaging conditions while strengthening recent ones. The recursive algorithm vota so may on the current input fingerprins the strengthening recent ones. The recursive algorithm vota so may on the current input fingerprins and storage space requirements and, therefore, enables our proposed approach to be online employed.

4 EXPERIMENTAL STUDIES

For a meaningful performance evaluation of our online fingerprint template improvement algorithm, the test database should contain not only a large number of finger IDs, but also a large number of the sample fingerprints per finger. Unfortunately, it is very difficult to find or build up such a database. Thus, we decided to conduct experiments with two different kinds of databases. The first experiment used the EVC2000 [22] databases that contain a large number of finger IDs and eight sample fingerprints per finger. The second experiment used a database collected by us that contains only 12 finger IDs but 2003 sample fingerprints per finger. The algorithm parameters chosen for both experiments were L = 8, $\alpha = 0.8$, $C_{\alpha} = 0.13$, $C_{\gamma} = 0.8$, May M = M = 0.25, and M = 10 = 0.8.

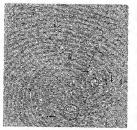
There are four databases, DB1_a, DB2_a, DB3_a, and DB4_a, used in FVC2000. Each database contains 100 finger IDs and eight fingerprints per finger (800 fingerprints in all). Let F; denote the minutia set extracted from the ith sample fingerprint of the ith finger, $i = 1, 2, \dots 8, j = 1, 2, \dots 100$. To test the verification performance with the unimproved template, each template T' = F', was matched against the inputs \mathbf{F}_{i}^{i} ($i < k \le 8$) to obtain the genuine matching scores and each template $T_1^1 = F_1^1$ was matched against the inputs \mathbf{F}_{i}^{1} $(j < k \le 100)$ to obtain the impostor matching scores. Let $\mathbf{T}_{i}^{i}(k)$ denote the improved template by using the original template F and six inputs \mathbf{F}_{i}^{m} $(1 \le m \le 8, m \ne i, m \ne k, i < k \le 8)$. To test the verification performance with the improved template, each improved template T'(k) was matched against the input F' to obtain the genuine matching score and each template $T_i^1(2)$ was matched against the inputs \mathbf{F}_{k}^{1} ($j < k \le 100$) to obtain the impostor matching scores. In both tests, a total of $((8 \times 7)/2) \times 100 = 2,800$ genuine matches and $(100 \times 99)/2 = 4.950$ impostor matches were performed on each database. These numbers of matches are the same as that used in the FVC2000 [22]. Fig. 1 illustrates the ROC curves on the four FVC2000 databases. These ROC curves on the four different

databases consistently show that our template improvement algorithm causes a significant improvement in the verification accuracy.

In the second experiment, a Veridicom CMCS sensor of size 300 x 300 pixels was used to capture fingerprins. Twelve untained users were enrolled by capturing one template fingerprint per user. Each of these 12 users was saked to represent the enrolled finger to the system to produce input fingerprints several times from one than five times) every working day until 199 input fingerprints per user were received. Each input fingerprint was marched online with the 12 template and used to update (online improve) the template that had the maximal matching score if this work of the control of

To show the template improvement progress clearly against the fingerprint input sequence, we averaged the results over the 12 users. Fig. 2 plots the average numbers of minutiae of the input fingerprints, the original templates, and the improved templates as well as the average numbers of improved template minutiae that were valid for matching. From Fig. 2, the improved template size increased with the first few fingerprint inputs and then stabilized at around twice the original unimproved template size. However, Fig. 2 also shows that the improved template had averaged fewer valid minutiae for matching than the original template. It means that, in most cases, the template improvement process removed more spurious minutiae compared with recovering dropped minutiae. This is because our minutia extraction algorithm, like most other minutia extraction approaches [6], usually produces more spurious minutiae than dropped minutiae. This experiment also tells us that the improved verification performance is not due to the increased number of minutiae in the improved template but the improved template quality.

Fig. 3 illustrates the average genuine matching scores may and the average imposter matching scores mais against the fingerprint input sequence. Fig. 3 clearly shows that the improved template produced not only higher genuine matching scores but also lower imposter matching scores that the improved template. Obviously, the higher genuine matching scores but do to the template improvement process. The lower imposter matching score also does not surprise us as the template improvement process reduced the number of spurious minutine and, thus, lowered the imposter matching scores is the process reduced the number of spurious minutine and, thus, lowered the imposter matching scores improved the fingerprint verification accuracy, as shown in Pig. 4.



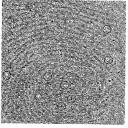


Fig. 5. (a) Original template minutiae and (b) improved template minutiae.

The average time taken by the fingerprint verification process (one minutia set extraction and one matching) was 0.147 seconds and the average time taken by the template improvement process was only 0.0003 seconds (for a Pentium III-733 MHz PC). Our template improvement algorithm only decelerates the fingerprint verification system by a negligible 0.2 percent.

Fig. 5a shows an original template minutia set while Fig. 5b shows the improved template minutia set (valid for matching, i.e., $\{F_k^p|c_k^p \ge 0.5\}$), generated using the template minutia set in Fig. 5a and 26 other input minutia sets. In these two figures, white dots represent endings, dark dots represent bifurcations, while white short lines represent the minutia directions. There are 30 minutiae in Fig. 5a and 32 minutiae in Fig. 5b. After the template improvement, five spurious minutiae were removed (see circles in Fig. 5a), seven dropped minutiae were recovered (see circles in Fig. 5b) and four minutiae had their type relabeled (see the arrows in Fig. 5a).

CONCLUSIONS

In this work, an online fingerprint template improvement algorithm is proposed. The proposed algorithm improves the reliability of a fingerprint template by using weighted averaging over all matched fingerprints that a fingerprint verification system receives. It reduces minutia extraction errors, such as spurious minutiae, dropped minutiae, and wrongly labeled minutia type, which are difficult to avoid using only a single fingerprint image. Furthermore, the template is gradually changed to reflect changes in the finger skin and imaging conditions by weighting recent fingerprints more heavily. A recursive algorithm minimizes the storage space and computation requirements of the template improvement process. As a result, the proposed fingerprint template improvement process can be performed online during the day-to-day operation of a fingerprint verification system. Extensive experimental studies demonstrate that the proposed online template improvement technique significantly increase the verification accuracy at a negligible cost in time. One problem of this technique is the enlargement of the template size. However, the improved template size is well limited to within twice the size of the original template.

REFERENCES

 A.K. Jain, L. Hong, and R. Bolle, "On-Line Fingerprint Verification," IEEE Trans. Pattern Analysis and Machine Intelligence, vol. 19, no. 4, pp. 302-314, Apr. 1997.

- A.K. Jain, L. Hong, S. Pankanti, and R. Bolle, "An Identity-Authentication System Using Fingerprints," Proc. IEEE, vol. 85, no. 9, pp. 1365-1388, Sept. 1997.

- 1907. X.D. Jiang, W.Y., Yau, and W. Ser, "Minutise Extraction by Adaptive Testing the Gray Level Radge of the Frageryntin Image," Proc. IEEE Steff. 1907. IEEE Steff. Image, "Proc. IEEE Steff. Image, Proc. IEEE Steff. Image, Proc. IEEE Steff. Image, Proc. IEEE Steff. Image, Proceeding for Adaptive Min. Image, Proc. IEEE Steff. Image, Proceeding for Image, Proc. IEEE Steff. Image, Image, Image, Image, Image, Imag
- Signal Processing, 1999.

 D. Maio and D. Maltonl, "Direct Gray-Scale Minutiae Detection in Fingerprints," IEEE Trans. Pattern Analysis and Muchine Intelligence, vol. 19,
- no. 1, pp. 27-39, 1997.

 R.M. Stock and C.W. Swonger, "Development and Evaluation of a Reader of Fingerprint Minutae," Technical Report CAL No. XM-2478-X-1: 13-17, Cornell Aeronautical Laboratory, 1969.
- B. Moayer and K. Fu, "A Tree System Approach for Fingerprint Pattern Recognition," IEEE Trans. Pattern Analysis and Machine Intelligence, vol. 8,
- Recognition, Inc. E. Imme. Manual Science (Recognition) in S. pp. 376-388, 1986.
 M.R. Verma, A.K. Majumdar, and B. Chatterjee, "Edge Detection in Fingerpoints," Pattern Recognition, vol. 20, no. 5, pp. 513-523, 1987.
- L. O'Gorman and J.V. Nickerson, "An Approach to Fingerprint Filter Design," Pattern Recognition, vol. 22, no. 1, pp. 29-38, 1989
- Coopin, "attern recognition, vol. 22, no. 1, pp. 39-38, 1989.

 XD, Jiang, W.Y. Yao, and W. Ser, "Detecting the Fingerprint Minutiae by Adaptive Tracing the Gray Level Ridge," Pattern Recognition, vol. 34, no. 5, pp. 599-1013, May 2001.

 XD, Jiang and W.Y. Yau, "Fingerprint Minutiae Matching Based on the Local And Global Structures," Prac. 18th 1nt1 Cost, Pattern Recognition,
- Local And Globa structures, Proc. 15th Int'l Conf. Pattern Recognition, vol. 2, pp. 1042-1045, 2000.
 Ch.M. Bishop, Neural Networks for Pattern Recognition. Oxford Univ. Press, 1995.
 P.J. Huber, Robust Statistics. New Yorks. John Wiley, 1981.
 L. Rabiner and J.B.-H. Juang, Fundamentals of Spaces Recognition. Premices
- Hall, 1993. Y. Bar-Shalom and T. Fortmann, Tracking and Data Association. Academic
- Press. 1988. G.E. Kopec and P.A. Chou, "Document Image Decoding Using Markov Soorce Models," IEEE Trans. Pattern Analysis and Machine Intelligence,
- 300rde bandens, IEEE Itaus, Fautern Annityso una sometime meetingenee, vol. 16, no. 6, pp. 602-617, June 1994.
 P. Magni, R. Bellazzi, and G.D. Nicolao, "Bayesian Function Learning Using MCMC Methods," IEEE Trans. Pattern Analysis and Machine
- Dailigence, vol. 20, no. 12, pp. 1319-1331, Dec. 1998.

 B. North, A. Blake, M. Isard, and J. Rittscher, "Learning and Classification of Complex Dynomics," IEEE Trans. Pattern Analysis and Macione
- of Complex Dynamics," IEEE Trans. Fattern Assayss and Maccome.
 Intiligency, vol. 22, no. 9, pp. 1016-1034, Sept. 1957.

 [20] K.A. Toh, W.Y. Yau, X.D. Jiang, T.P. Chen, J. Lu, and E. Lim, "Minutiae
 Data Synthesis for Pingerparia Identification Application," Proc. IEEE Int'l
 Conf. Image Processing, 2001.

 [21] R.C. Gonnates and R.E. Woods, Digital Image Processing. Addison Wesley,
 R.C. Contacts and R.E. Woods, Digital Image Processing.
- [22] D. Maio, D. Maltoni, R. Cappelli, J.L. Wayman, and A.K. Jain, "FVC2000: Pingerprint Verification Competition," Proc. 15th Int'l Conf. Pattern Recognition, 2000.



Available at www.ElsevierComputerScience.com POWERER BY SCIENCE @DIRECTY

Pattern Recognition 37 (2004) 1533--1542



Biometric template selection and update: a case study in fingerprints

Umut Uludaga, Arun Rossb,*, Anil Jaina

³ Department of Computer Science and Engineering, Michigan State University, East Lansing, M1 48824. USA ⁵ Department of Computer Science and Electrical Engineering, West Virginia University. Morgoniown, WV 26506, USA

Received 23 June 2003; accepted 13 November 2003

Abstract

A biometric authentication system operates by acquiring biometric data from a user and comparing it against the template data stored in a database in order to identify a person or to verify a claimed identify. Most systems store multiple templates per user in order to account for variations observed in a person's biometric data. In this paper we propose two methods to perform automatic template selection where the goal is to select prototype fingerprint templates for a finger from a given set of fingerprint intemposasions. The first method, called DEND, employs a clustering strategy to choose a template set that best represents the inter-class variations, while the second method, called DEND, entry the second method, called DEND, entry the second method, called DEND, and the second method, called DEND, and the second method, called DEND, and the second method and the second method and the second method, called DEND, and the second method, called DEND, and the second method and the second method, called DEND, and the second method and the se

2003 Pattern Recognition Society. Published by Elsevier Ltd. All rights reserved.

Kepwords: Biometries; Template selection: Template update; Fingerprints; Clustering; Prototype; Template aging

1. Introduction

A biometric authentication system uses the physiological (ingerpriats, fee, band geometry, ints) and/or behavioral (ingerpriats, fee, band geometry, ints) and/or behavioral (voice, signature, keystroke dynamics) traits of an individual to identify a person or verify a claimed identify [1]. A phical biometric system operates in two distinct stages, the caroliment stage and the authentication stage. During molliment, a user's biometric data (e.g., fingerprints) is acquired and processed to extract a feature set (e.g., minutriate points) that is stored in the database. The stored feature set, is beliefled with the trace's identify, is referred to as a template, in order to account for variations in the biometric data of

0031-3203/830.00 № 2003 Pattern Recognition Society. Published by Elsevier Ltd. All rights reserved. doi:10.1016/j.patcog.2003.11.012

a user, multiple templates corresponding to each user may be stored. During authentication, a user's biometric data is once again acquired and processed, and the extracted feature set is matched against the template(s) stored in the database in order to identify a previously enrolled individual or to validate a claimed identity. The matching accuracy of a biometries-based authentication system relies on the stability (permanence) of the biometric data associated with an individual over time. In reality, however, the biometric data acquired from an individual is susceptible to changes due to improper interaction with the sensor (e.g., partial fingerprints, change in pose during face-image acquisition), modifications in sensor characteristics (e.g., optical vs. solid-state fingerprint sensor), variations in environmental factors (e.g., dry weather resulting in faint fingerprints) and temporary alterations in the biometric trait itself (e.g., cuts/scars on fingerprints). In other words, the biometric measurements tend to have a large intra-class variability. Thus, it is possible for the stored template data to be significantly different

Corresponding author. Tel.: +1-304-293-0405; fax: +1-304-293-8602.

E-mail addresses: uludagum@ese.msu.edu (U. Uludag), ross@esee.wvu.edu (A. Ross), jain@ese.msu.edu (A. Jain).



Fig. 1. Intra-class variation in fingerprints. (a) Two impressions of the same finger separated by a period of 6 weeks exhibiting difference in moisture content. (b) Two impressions of the same finger acquired using different sensors (solid-state and optical). (c) Two impressions of a fingerprint exhibiting partial overlap.

from those obtained during anthentication (see Figs. 1-3), resulting in an inferior performance (higher false rejects) of the biometric system.

In order to account for the above variations, multiple templates, that best represent the variability associated with a user's biometric data, should be stored in the database. For example, one could store multiple impressions pertaining to different portions of a user's fingerprint in order to deal with the problem of partially overlapping fingerprints. Similarly, a user's face image acquired from multiple viewpoints only be stored in order to account for variations in a person's one. There is a tradeoff between the number of templates,

and the storage and computational overheads introduced by multiple templates. For an efficient functioning of a biometric system, the process of template selection has to be automated. However, there is limited literature dealing with the problem of automatic template selection in a biometric system. In this paper we propose techniques to perform antomatic template selection. The methods presented here attempt to represent the variability as well as the typicality observed in a user's biometric data. The proposed methods have also been utilized to perform automatic template update. Our experimental results indicate the importance of adopting a formal procedure to perform template selection and update. Although we consider a fingerprint-based biometric system as our test-bed, the techniques presented in this paper may be applied to other types of biometric traits (such as face and hand geometry) as well.

The rest of the paper is organized as follows. In Section 2 the two methods used to perform template selection have been described. In Section 3 the methodologies used to perform template update have been explained; Section 4 describes the experiments conducted to study the effectiveness of the proposed lechniques; Section 5 summarizes the results of this work and provides future directions for research.

2. Template selection

The problem of template selection with regard to fingerprints may be posed as follows: Given a set of M fingerprint images corresponding to a single finger, select K templates that 'best' represent the variability as well as the typicality observed in the Minages, K - Ni. Curroutly, we settlement that the value of K is predetermined. This systematic selection of templates is expected to result in a better performaof a fingerprint matching system compared to a random selection of K templates out of the N images.

It is important to note that template selection is different from template update. The term template update is used to refer to one of the following situations: (i) Template aging: Certain biometric traits of an individual vary with age. The hand geometry of a child, for example, changes rapidly during the initial years of growth. To account for such changes, old templates have to be regularly replaced/augmented with newer ones. The old templates are said to undergo aging. (ii) Template improvement: A previously existing template may be modified to include information obtained at a more recent time instance. For example, minutiae points may be added to, or deleted/modified from the template of a fingerprint, based on information observed in recently acquired impressions [3-5]. As another example, Liu et al. [6] update the eigenspace in a face recognition system via decay parameters that control the influence of old and new training samples of face images. Thus, template selection refers to

¹ Template selection has been studied in the context of other pattern recognition problems (see Ref. [2], for example).



Fig. 2. Intra-class variation associated with an individual's face image. Due to change in pose, an appearance-based face recognition system will not be able to match these three images successfully, although they belong to the same individual [12].

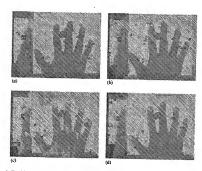


Fig. 3. Hand images of an individual acquired over a period of 4 years using the same hand reader [13].

the process by which prototype templates are chosen from a given set of samples, whereas template update refers to the process by which existing templates are either replaced or modified. In the next section, we present techniques for template update, based on the template selection methods presented in this section.

We propose the following two methods for template selection:

Method 1 (DEND): In this method, the N fingerprint impressions corresponding to a user are grouped into K clusters, such that impressions within a cluster are more similar than impressions from different clusters. Then for each cluster, a prototype (prepresentative) impression that tryfiles the members of that cluster is chosen, resulting in K template impressions. This technique, therefore, selects prototypes that represent the variability observed in the impressions.

To perform clustering, it is required to compute the (disjainilarity between fingerprint impressions. This measure of (disjainilarity is obtained by matching the minutine point sets of the fingerprint impressions. Our matching algorithm is based on an elastic string matching technique [7], and it outputs a distance score indicating the dissimilarity of the minutie sets being compared. We use a simple matching algorithm since our goal is to perform template selection, regardless of the characteristics of the matching algorithm.

Since our representation of the N fingerprint impressions is in the form of a $N \times N$ dissimilarity matrix instead of a $N \times N$ distimilarity matrix instead of a $N \times N$ pattern matrix (d is the number of features), we use hierarchical clustering [8]. In particular, we use an agguernettive complete link clustering algorithm. The output of this algorithm is a dendrogram which is a binary tree, where each terminal node corresponds to a fingerprint impression, and the intermediate nodes indicate the formation of clusters (see Fig. 4).

The template set T, |T| = K, is selected as follows:

Step 1: Generate the $N \times N$ dissimilarity matrix, M, where entry (i, j), $i, j \in \{1, 2, ..., N\}$ is the distance score between impressions t and j.

Step 2: Apply the complete link clustering algorithm on M, and generate the dendrogram, D. Use the dendrogram D to identify K clusters.

Step 3: In each of the clusters identified in step 2, select a fingerprint impression whose average distance from the rest of the impressions in the cluster is minimum. If a cluster has only 2 impressions, choose any one of the two impressions at random.

Step 4: The impressions selected in step 3 constitute the template set T.

In Step 2, the algorithm automatically determines the metabold distance to cut the dendrogram and identify excelly K clusters. For example, for the dendrogram given in Fig. 4, this distance is determined to be 644. We refer to the above algorithm as DED since it uses the dendrogram to choose the representative templates. The algorithm selects prototypes that represent the eartholity observed in a user's data. Therefore, this algorithm is prone to selecting outliers.

Method 2 (MDIST): The second method sons the fingerpriot impressions based on their average distance scere with other impressions, and electes those impressions that correspond to the K smallest average distance sceres. Here the rationale is to select templates that exhibit maximum similarit with the other impressions and, bence, represent typical data measurements. We refer to this method as MDIST since templates are chosen using a minimum distance criteria. The prototype set selected by this technique represents data that is likely to occur frequently. Thus, for every user:

Step 1: Find the pair-wise distance score between the N impressions.

Step 2: For the jth impression, compute its average distance score, d_j, with respect to the other (N-1) impressions. Step 3: Choose K impressions that have the smallest average distance scores. These constitute the template set T.

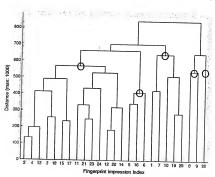


Fig. 4. Dendrogram generated using the 25×25 dissimilarity matrix of a finger. The circles on the subtrees indicate cluster formations for K = 5.

The choice for the value of K is application dependent. Larger K values would mean aforing mare templates per user, and this may not be feesible in systems with limited storage expacties. Moreover, in an identification system, matching a query (input) data with a large number of templates per user would be computationally demanding. Smaller K values, on the other hand, may not sufficiently capture the intra-class variability nor the typicality of the data, leading to inferior matching performance. Therefore, a reasonable value of K, that takes into account the aforementational felories, bus to be specified.

3. Template update

The methods presented in the previous section on the applied periodically in order to pedient the currently selected template set. In a biometric system, a user provides biometric date every time the authentication stage is invoked. Thus, news samples of a user's biometric are made available over a period of time. This newly senjored data can be used to refrest the current template set in order to account for temporal changes that may occur in a person's biometric tust. We suggest two simple methods to perform template undate using the newly accumined and

In the list method, all current templates are replaced with emplates selected from the newly acquired data set, thereby capturing temporal changes in the fingerprints (e.g., cheups due to environmental conditions, sensor chameteristics so sobject's occupational chameteristics). We call this method BATGTI-1PDATE since the previously selected batch is discarded and only the unewly acquired data is considered.

In the second melhod, both the current template set and the newly obtained data set are considered when performing template update. The template selection procedure is applied after augmenting the new data set with the current template set. This method is called AUGENTI-UPDATE. We provide experimental results pertaining to both these update methodologies in the next section.

The template selection and update procedure can be invoked on each user independently and is not affected by the variable number of biometric samples available for a user. Moreover: It is an off-line process that does not interfere with the real-time perfurmance of a system. As a result, the procedure can be easily scaled to accommodate a large number of users.

4. Experimental results

In order to study the effect of automatic template selection and update on lingerprint matching, it is necessary to sequire several impressions per finger over a period of time. Standard fingerprint databases (e.g., FVC 2002 [9]) do not contain a large number of impressions per finger. Therefore, we collected 200 impressions each of 50 different fingers in our bhoratory using the Identix Bir-Touch 1953 200 optical sensor (255 × 256 images, 330 opt). The data was acquired over a period of approximately four monetal with no more than 5 impressions of a finger per day. The 200 impressions of each linger were partitioned into the template solution experiments while the remaining 100 impressions (DATA) were under the complete selection experiments while the remaining 100 impressions (DATA) where the probability of the complete selection experiments while the remaining 100 impressions in the foundation of the complete selection of these two sets were further divided into timing (first 25 impressions) and test (remaining 75 impressions) sets. These individual partitions were labelled at ThALFSI, TESTI.

4.1. Template selection

The template selection experiments were conducted using DATA1. The selection procedure was applied to images in TRAIN1, while the matching performance was evaluated using images from TEST1.

Fig. 4 shows the dendrogram obtained using the 25 fingerprint impressions of one finger. Ou setting K=5, the resulting clusters and their prototypes as computed using the DBMO algorithm are shown in Fig. 5; some clusters are seen to have only one numbers, agreesting the existence of outliers. The various prototypes are observed to have different regions of overlap with respect to the extracted minutiae points. The prototypes, for the same finger, computed using the MDTST algorithm are shown in Fig. 6.

In order to assess the matching performance of the pronosed techniques (for K = 5), we match every image in TEST1 (50 fingers, 75 impressions per finger) against the selected templates (5 per finger). When a test image is matched with the selected template set of a finger, 5 different distance scores are obtained. The mean of these scores is reported as the final matching score.2 Thus, we obtain 187, 500 matching scores $(75 \times 50 \times 50)$ using the selected template sets. Fig. 7(a) shows the receiver operating characteristic (ROC) curves representing the matching performance of the template sets selected using both the algorithms. The equal error rates (EER) of DEND and MDIST are observed to be 7.42% and 6.62%, respectively. Now, for the 50 fingers, there are a total of $\binom{25}{5}^{50} - 1$ non-selected template sets. It is computationally prohibitive to generate the matching scores and the ROC curves corresponding to all these permutations. Therefore, we chose 53,130 permutations (assuming that the impression indices in the template set of all the 50 fingers is the same) and computed their EER. The histogram of EER values is shown in Fig. 7(b), where the minimum. mean and maximum EER values are 6.12%, 7.89% and 10.31%, respectively. In this histogram, the vertical lines indicate the EER values corresponding to the DEND and MDIST

²Other techniques to combine matching scores can be found in Ref. [10].

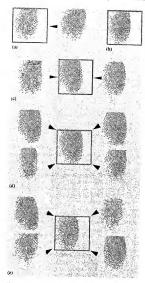


Fig. 5. The cluster membership (K = 5) for the dendrogram shown in Fig. 4. At most 5 members are indicated for each cluster. The prototype template in each cluster is marked with a thick border. Note that the cluster in (b) has only one member.

algorithms. The percentage of non-selected template sets that have a lower EER than the template sets selected with the proposed methods is 30.3% and 1.6%, for DEND and MDIST, respectively, thereby suggesting that systematic template selection is better than random selection.

We see that the MDIST method of template selection leads to a better matching performance compared to the DEND method of selection. This may be attributed to the fact that MDIST selects a template set consisting of images that exhibit maximum similarity with other impressions: therefore, the probability of them bring correctly matched with impressions of the same flager is furily high. On the other hand, the Digith method is prone to selecting impressions that are outliers thereby increasing the probability of false rejects. However, both methods are essential the to the complementary nature of the template set that they select.

To further understand the differences and similarities between the empirise rest selected by the BDOs and the between the template rest selected by the BDOs and the selected using these two methods (so Ker Es). The minimum, average (over all 20 users) and the maximum valens for that number is Bund to be 0, 1.54 and 5, respectively. Since, on the average, 1.54 out of a possible 5 impressions are common in the selected selects, the difference in performance between the two techniques stems from the remaining members of the respective acts.

Table 1 liets the impressions of a finger that were selected as templates using the DBM and 10 TST algorithms at different K values. The impression index indicates the acquisition time of the impression index and indicate the acquisition time of the impression index and its officer relationship between an impress that there is discretely an experimental products of K and the choice as a template. Fig. 8 shows the EBRs of the computational content of the computation of the comput

4.2. Template update

In this subsection, we report the system performance of the BATCS—PDATS and ADOMEST—PDATS untbods. Observe that both these update techniques implicitly really on the template selection procedures described outlier. They differ only in the choice of the data set ou which template selection is performed. To demonstrate the apportance of template update, we report the marching performance before and after the update process. We assume that the current template set of a finger consists of images from TRAINI.

In the BATCH-UPDATE method, template selection was performed on TRAID2 after completely discarding the template set extracted from TRAID1. The MADERAT-PUBATE method, on the other hand, images from TRAID2 were first augmented with the 5 current templates, and template selection was performed on the augmented sel. Both the public techniques selected 5 templates from their respective candidate sets. The matching performance of the two update techniques was evaluated using data set TBSTZ. Fig. 9 shows the ROC curves indicating the performance before template update (i.e., templates selected from TRAID1



Fig. 6. The prototype templates of a finger selected using the MDIST algorithm. The average distance measures for there are (a) 425, (b) 429, (c) 431, (d) 441, and (e) 452.

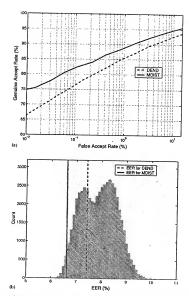


Fig. 7. (a) The ROX' curves for the DEND and NDLST algorithms on a database of 50 fingers with 75 impressions per finger used in the test phase. (b) The EER histogram for the non-netected sets. The EER of the DEND and MDLST algorithms are also indicated.

BNSDOCID «XP_____4508402A_I_>

Table 1 The impression indices of selected templates for a finger at different values of K

K	DEND	HDIST
1	2	2
3	4, 8, 25	2. 4. t3
5	4, 5, 9, 22, 25	2, 3, 4, 12, 13
7	2. 5. 7. 9, 19, 22, 23	2. 3. 4, 12, 13, 21, 23
9	2, 5, 7, 8, 9, 19, 20, 22, 23	2, 3, 4, 12, 13, 20, 21, 23, 25

were tested on TEST2) and after incorporating the template update procedures. Table 2 lists the EERs of both the update methods based ou the selection technique (DEM) and MDIST) that was employed. It is seen that both the update methods result in substantial improvement in matching performance.

We observe from the ROC curves and EER values that AURENT-UPDATE results in better performance than BATCH-UPDATE. This is because in AURENT-UPDATE we give the previously selected templates a chance to compete for reselection. This can bely in retaining long-term trends in the characteristics of the fingerprint impressions leading to the observed improvement in performance. In AURENT-UPDATE, the average number of nestlected templates (the average is taken over 50 users) was found to be 1.5 and 0.62 using the DEND and MDIST methods, respectively.

5. Discussion and future work

A systematic procedure for template selection and update is critical to the performance of a biometric system. In this paper we have proposed two techniques to perform template selection in the context of a fingerprint matching system. Both techniques are based on the distance score between pairs of fingerprint impressions originating from the same finger. The first method called DEND utilizes a clustering scheme to detect prototype impressions. The template set selected by this technique captures the variability observed in a user's fingerprint image. The second method called MDIST ranks the fingerprint impressions based on their average distance from the other impressions, and then selects impressions whose average distance is the least. Thus, it aids in selecting a template set that exhibit maximum similarity with the other impressions. Our experiments demonstrate that a systematic template selection procedure results in better performance than random template selection; it was also observed that the MDIST technique results in better performance than DEND. Currently, we are studying ways to effectively combine the two techniques in order to further improve system performance. We are also considering methods to determine the value of K automatically.

We have also proposed two template update mothods that refresh the current template set based on newly acquired biometric data. The update methods implicitly rely on the template selection process. The AUGMENT-UPDATE technique performs template selection by considering both the current

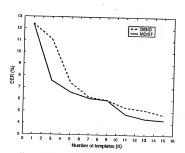


Fig. 8. The EER of the fingerprint matcher plotted as a function of K.

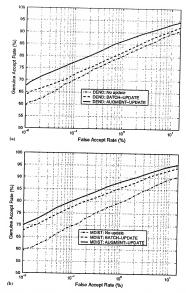


Fig. 9. ROC curves showing improvement in performance when the BATCH-UPDATE and AUGRERT-UPDATE procedures are incorporated. In (a) the DERD method of template selection was used, while in (b) the RDIST method was employed.

template set as well as the newly acquired data set. The BATCH-UPDATE lechaique, on the other hand, considers and BATCH-UPDATE lechaique, on the other hand, considers with the newly acquired data set and completely diseards the current template set. Both the update methods were shown to improve the mething performance of the system. Our experiments indicate that AUGHSTI-UPDATE; yields better matching performance than BATCH-UPDATE.

It must be mentioned that the template selection and update techniques described here are based on the distance measure (scores) between pairs of fingerprint impressions. We have therebre, adopted a featureless approach to class-teing [11]. Hence, if a different fingerprint maching algorithm is used, a different set of prototype impressions is likely to be oblained. We are developing alternate techniques when would operate on the raw images in order to detect proye impressions. We are also in the process of testing our techniques on other hometric modalities as well (viz., face and land geometry).

Table 2
EER values before and after incorporating the template update

procedure			
Update technique		EER (%)	
DEND method	,	***************************************	
No update		10.61	
BATCH-UPDATE		9.55	
AUGHENT-UPDATE		7.37	
MDIST method			
No update		10.32	
BATCH-UPDATE		7.69	
AUGMENT-UPDATE		6.31	

Acknowledgements

This project was sponsored in part by the Center for Identification Technology Research (CTTeR, West Virginia)—a Industry-University Cooperative Research Center (IUCRC) funded by the National Science Foundation (NSF).

References

- A.K. Jain, R. Bolle, S. Pankanti (Eds.), Biometrics: Personal Identification in Networked Society, Kluwer Academic Publishers, Dordrocht, 1999.
- [2] S.D. Connell, A.K. Jain, Template-based online character recognition, Pattern Recognition 34 (1) (2001) 1-14
- [3] X. Jiang, W. Ser, Online fingerprint template improvement, IEEE Trans. PAMI 24 (8) (2002) 1121-1126.

- [4] K.A. Toh, W.Y. Yau, X.D. Jiang, T.P. Chen, J. Lu, F. Lim, Minutiae data synthesis of fingerprint identification applications, in: Proceedings of the International Conference on Image Processing (ICIP), Thessaloniki, Greece, Vol. 3, 2001, pp. 262–265.
- [5] A.K. Jain, A. Ross, Fingerprint mosaicking, in: Proceedings of IEEE International Conference on Acoustics, Speech, and Signal Processing (ICASSP), Orlando, Florida, 2002.
- [6] X. Liu, T. Chen, S.M. Thornton, Eigenspace updating for non-stationary process and its application to face recognition, Pattern Recognition, Special issue on Kernel and Subspace Methods for Computer Vision (2003) 1945–1959.
- [7] A.K. Juin, L. Hong, R. Bolle, On-line fingerprint verification, IEEE Trans. PAMI 19 (4) (1997) 302-314.
- [8] A.K. Jnin, R.C. Dubes, Algorithms for Clustering Data, Prentice-Hall, Englewood Cliffs, NJ, 1988.
- [9] D. Maio, D. Maltoni, R. Cappelli, J.L. Wayman, A.K. Jain, FVC2002: Fingerprint verification competition, in: Proceedings of the International Conference on Pattern Recognition (ICPR), Quebec City, Canada, 2002, pp. 744–747.
- [10] J. Kittler, M. Hatef, R.P. Duin, J.G. Matas, On combining classifiers, IEEE Trans. PAMI 20 (3) (1998) 226-239.
- [11] R.P. Duin, D. de Ridder, D.M.J. Tax, Experiments with a featureless approach to pattern recognition, Pattern Recognition Lett. 18 (1997) 1159-1166.
- [12] R.-L. Hsu, Face detection and modeling for recognition, Ph.D. Thesis, Michigan State University, 2002.
- [13] A.K. Jais, A. Ross, S. Pankanti, A prototype land geometry-based verification system, in: Second International Conference on Audio and Video-based Blometric Person Authentication (AVBPA), Washington, DC, USA, 1999, pp. 166-171.

About the Author—UNUT ULUDAG received B.S. and M.S. degues in Electrical and Electronics Engineering from Bogaziat (Luiveuty, Instantol, Turkey, in 1999 and 2001, respectively). He was a researcher in Marman Research Ceast, Turkey, from 1999 to 2001. He is now a Ph.D. studed in Department of Computer Sections and Engineering, Michigan State University, East Luxing, M.H. His research interest inducted biometrics, postern recognition, westermenting, and infinitely, inserpe processing and computer vision. He is a emember of the IEEE.

About the Auther—ARIN ROSS is an Assistant Professor in the Lane Department of Computer Science and Electrical Engineering of West Virginia University. Ross received his Res. El (1968) degree in Computer Science from the Bird Institute of Technology and Science, Plann (India), in 1996. He obtained his M.S. and P.D. degree in Computer Science and Engineering from Michigan State University in 1999 and 2000, respectively. Between July 1996 and December 1997, he worked with the Design and Development group of That Elexi (India) Lud, in Bangalore. He also speed three numers 12000–2002) with the Imaging and Virginization group at Science Corporation. Science Corporation, Inc. Princeton, working on fingerprint recognition algorithms. His research increase include statistical pattern recognition, image processing, computer vision and biometric authentication.

About fine Anthur—ANIL JANI is a University Distinguished Professor in the Departments of Computer Science & Engineering and Decrited and Computer Engineering at Meliting State University. His neason's interests include statistical pattern accepation, exploratory pattern analysis, Markov random fields, texture analysis, 20 object recognition, medical image analysis and bamedic authentication. Several of his papers have been reprinted in edited volumes on image processing and pattern recognition. Its received the best paper avaroats in 1978 and 1991, and received earthers from the Pattern Recognition Society. He also received the thest paper avaroats in 1978 1979 and 1995, 1997 and 1995 from the Pattern Recognition Society. He also received the third part of Pattern Recognition Society. He also received the United Society and Pattern Recognition (JARY), he has received a Full-bright Research Award, a fellow of the HEEP, CAM, and International Association of Pattern Recognition (JARY) has the accessful and the Pattern Recognition (Fall-Wise Heep). The pattern and the patt

BNSDOCID: «XP_____4508402A__I_>